

## 5 Rationale Zahlen

### 5.7 Übungen Frommenwiler

$$45. \quad b) \quad \frac{x-5}{y-4x} \cdot \frac{(-1)}{(-1)} = \frac{-x+5}{\underline{\underline{4x-y}}}$$

$$c) \quad \frac{pq}{p+q} \cdot \frac{q-p}{q-p} = \frac{pq^2 - p^2q}{\underline{\underline{q^2 - p^2}}}$$

$$d) \quad \frac{5x}{3x-2} \cdot \frac{3x+2}{3x+2} = \frac{15x^2 + 10x}{\underline{\underline{9x^2 - 4}}}$$

$$46. \quad b) \quad \frac{4-a}{1-a} \cdot \frac{(-1)}{(-1)} = \frac{a-4}{\underline{\underline{a-1}}}$$

$$d) \quad \frac{-a(a-1)}{-b} \cdot \frac{(-1)}{(-1)} = \frac{a(a-1)}{b} = \frac{a^2 - a}{\underline{\underline{b}}}$$

$$e) \quad \frac{(n-1)(n-2)}{-n} \cdot \frac{(-1)}{(-1)} = \frac{(1-n) \cdot (n-2)}{\underline{\underline{n}}} \quad \text{oder} \quad \frac{(n-1)(2-n)}{\underline{\underline{n}}} \quad \text{oder} \quad \frac{-n^2 + 3n - 2}{\underline{\underline{n}}}$$

$$f) \quad \frac{(x-y)^2}{-x-y} \cdot \frac{(-1)}{(-1)} = \frac{(x^2 - 2xy + y^2)(-1)}{x+y} = \frac{-x^2 + 2xy - y^2}{\underline{\underline{x+y}}}$$

$$47. \quad a) \quad \frac{\cancel{a}^2 a(a-b)}{\cancel{a}^2 (a^2 - 2ab + b^2)} = \frac{2a \cancel{(a-b)}}{(a-b)^2} = \frac{2a}{\underline{\underline{a-b}}}$$

$$c) \quad \frac{a+b-a^2}{a+b} \rightarrow \text{der Zähler kann nicht faktorisiert werden!}$$

**somit:**  $\rightarrow$  der Bruch kann nicht gekürzt werden!

$$d) \frac{(x-y)(x+y)(-1)}{(y-x)(y-x)(-1)} = \frac{\cancel{(x+y)}(x+y)}{\cancel{(y-x)}(-y+x)} = \frac{x+y}{\underline{\underline{x-y}}}$$

$$f) \frac{(-1)(d^2 + cd - 12c^2)}{(d-5c)(d+4c)} = \frac{(-1)(\cancel{d+4c})(d-3c)}{(d-5c)\cancel{(d+4c)}} = \frac{3c-d}{\underline{\underline{d-5c}}}$$

$$48. a) \frac{x^2(x^2 - 4x + 4)}{x(x^4 - 8x^2 + 16)} = \frac{x(x-2)^2}{(x^2-4)^2} = \frac{x(x-2)^2}{[(x-2)(x+2)]^2} = \frac{\cancel{x(x-2)^2}}{(\cancel{x-2})^2(x+2)^2} = \frac{x}{\underline{\underline{(x+2)^2}}}$$

$$c) \frac{\overbrace{(x-y)^2 - z^2}^{\text{Binomtyp: } a^2 - b^2}}{(\underbrace{x+z)^2 - y^2}_{\text{Binomtyp: } a^2 - b^2}} = \frac{[(x-y)-z][(x-y)+z]}{[(x+z)-y][(x+z)+y]} = \frac{(x-y-z)\cancel{(x-y+z)}}{(\cancel{x-y+z})(x+y+z)} = \frac{x-y-z}{\underline{\underline{x+y+z}}}$$

$$d) \frac{(a^2-1)(a^2+1)}{a^2(a+1)+a+1} = \frac{(a-1)(a+1)(a^2+1)}{a^2(a+1)+1(a+1)} = \frac{\cancel{(a+1)}(a-1)\cancel{(a^2+1)}}{\cancel{(a+1)}(a^2+1)} = \underline{\underline{a-1}}$$

$$e) \frac{2u(2u-3)}{2(4u^3 - 8u^2 - 9u + 18)} =$$

$$\frac{2u(2u-3)}{2[4u^2(u-2) - 9(u-2)]} =$$

$$\frac{2u(2u-3)}{2(u-2)(4u^2-9)} =$$

$$\frac{\cancel{2u(2u-3)}}{\cancel{2}(u-2)\cancel{(2u-3)}(2u+3)} = \underline{\underline{\frac{u}{(u-2)(2u+3)}}}$$

$$f) \frac{(3n+2)(n+2)}{(n-2)^2} \rightarrow \text{kann nicht gekürzt werden!}$$

$$\begin{aligned}
 49. \quad a) \quad & \frac{a^2 - b^2 + ax - bx}{a^2 - \underbrace{(b^2 + 2bx + x^2)}_{\text{Binom}}} = \\
 & \frac{(a-b)(a+b) + x(a-b)}{\underbrace{a^2 - (b+x)^2}_{\text{Binomtyp: } a^2 - b^2}} = \\
 & \frac{(a-b) \cancel{[(a+b) + x]}}{\cancel{[a - (b+x)]} \cancel{[a + (b+x)]}} = \underline{\underline{\frac{a-b}{a-b-x}}}
 \end{aligned}$$

$$\begin{aligned}
 b) \quad & \frac{(p-q) \left[ -2(p+q)(p-q) + (p-q)^2 + (p+q)^2 \right]}{5p^2(p^2 - 2pq + q^2)} = \\
 & \frac{\cancel{(p-q)} \left[ -2(p+q)(p-q) + (p-q)^2 + (p+q)^2 \right]}{5p^2(p-q)^2} = \\
 & \frac{-2(p^2 - q^2) + p^2 - 2pq + q^2 + p^2 + 2pq + q^2}{5p^2(p-q)} = \\
 & \frac{-2p^2 + 2q^2 + p^2 - 2pq + q^2 + p^2 + 2pq + q^2}{5p^2(p-q)} = \underline{\underline{\frac{4q^2}{5p^2(p-q)}}}
 \end{aligned}$$

oder

$$\begin{aligned}
 & \frac{(p-q) \left[ \underbrace{-2(p+q)(p-q) + (p-q)^2 + (p+q)^2}_{\text{Binom: } (\quad)^2 - 2(\quad)(\quad) + (\quad)^2 = [(\quad) - (\quad)]^2} \right]}{5p^2 \underbrace{(p^2 - 2pq + q^2)}_{\text{Binom}}} = \\
 & \frac{\cancel{(p-q)} \left[ (p-q) - (p+q) \right]^2}{5p^2(p-q)^2} = \frac{[p-q-p-q]^2}{5p^2(p-q)} = \frac{(-2q)^2}{5p^2(p-q)} = \underline{\underline{\frac{4q^2}{5p^2(p-q)}}}
 \end{aligned}$$